

# An overview of past and current ocean data assimilation efforts at the US Naval Research Laboratory (NRL)

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## **INTRODUCTION**

Numerical models have matured over the years and are now simulating the ocean at very high resolution.

Ocean forecasts still contain errors, especially at smaller scales, due to various sources: boundary conditions (for regional models), external forcing, parameterizations of physics and unresolved processes.

The evolution of ocean DA at NRL also includes the types of observations, as well as how sea surface height (SSH) observations have been projected to the interior: from statistical inference and Cooper-Haines to synthetic profiles and direct assimilation.

Over the past few decades, the U.S. Naval Research Laboratory (NRL) has implemented progressively advanced data assimilation methods (from univariate optimal interpolation to 3D and 4D variational techniques) with increasingly sophisticated models (the Navy Layered Ocean Model (NLOM), the Navy Coastal Ocean Model (NCOM), the Hybrid Coordinate Ocean Model (HYCOM)), ice and waves (SWAN, WW3).







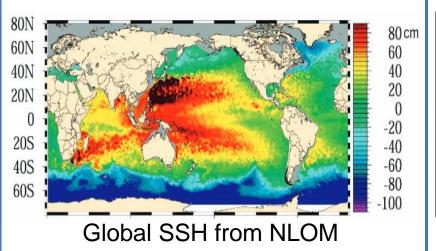




## THE MODELS

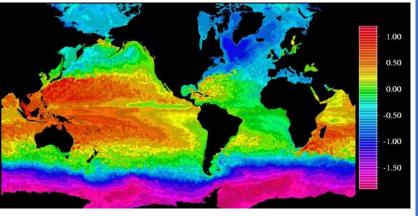
#### **NLOM**

Primitive equation layered model Free surface, eddy-resolving 72S-65N, no polar latitudes Depths > 200m 1/16 and 1/11.4 lat-lon resolution 6 vertical layers



#### **NCOM**

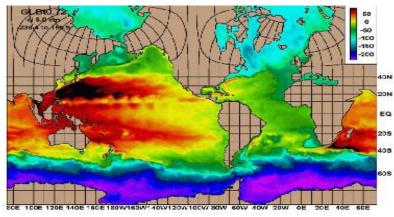
Primitive equation layered model Free surface, eddy-permitting 80S-Arctic cap Depths > 5m 1/8 lat-lon resolution 41 sigma-z vertical layers



Global SSH from NCOM

#### **HYCOM**

Primitive equation layered model Free surface 86S-Arctic cap Depths > 5m 1/25 lat-lon resolution 41 hybrid vertical layers



Global SSH from HYCOM











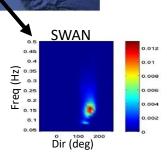
## THE MODELS

#### **SWAN**

Third generation spectral wave model for nearshore, based on the wave action balance equation with sources and sinks.

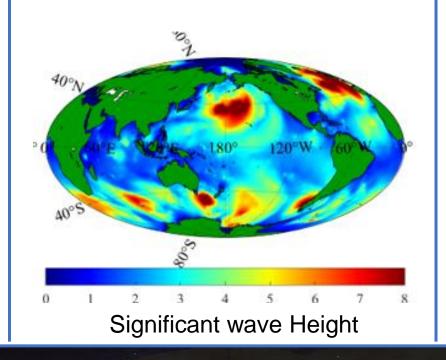
SWAN Assimilation Domain & Mini-Buoy Array





#### WAVEWATCH3

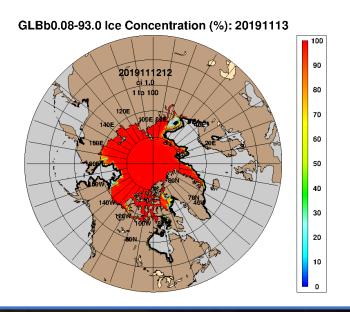
Third-generation phase-averaged wave model solving for spectral action-density
1/2 to 1/10<sup>th</sup> degree resolution



#### CICE

From Polar Ice Prediction System (PIPS) 127 km to 27 km

CICE at 1/12<sup>th</sup> coupled with HYCOM
Get info from David Hebert











## DA METHODS: OCEAN

- Navy Coupled Ocean Data Assimilation System (NCODA)
- Cycling Analysis-Forecast-Analysis system using the incremental analysis update method

#### **Ocean**

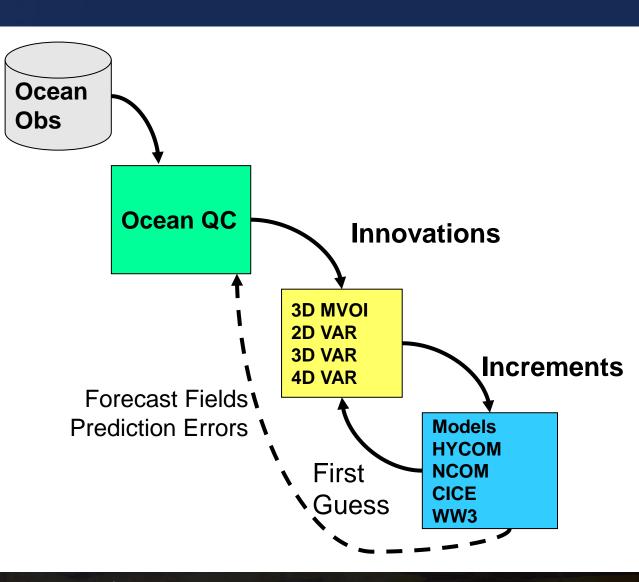
- SST (sat & buoy)
- SSHA (Nadir and SWOT altimeters)
- T/S profiles (CTD, XBT, float, glider)
- Velocity profiles (ADCP)
- Surface currents (drifters, HF radar)

#### **Wave**

- Significant wave height
- Wave spectra (in progress)

#### CICE

- Ice concentration
- Ice thickness (in progress)







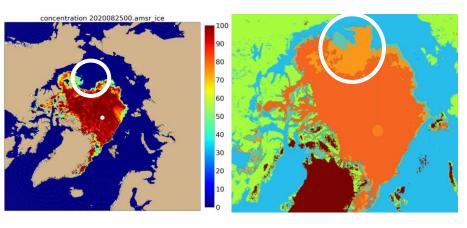


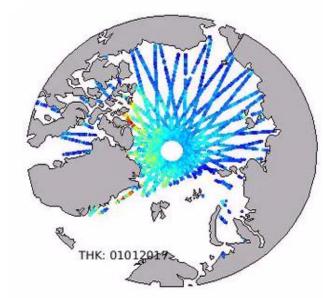


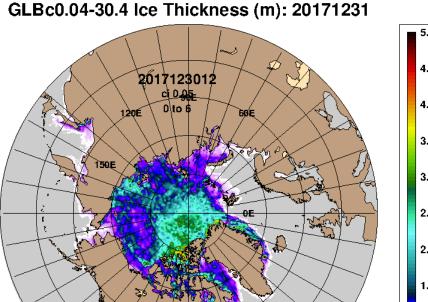


2D assimilation of concentration from SSMI and AMSR2 supplemented by the Interactive Multisensor Snow and Ice Mapping System (IMS)

We are currently testing and validating the assimilation of Ice thickness from CryoSat







Combined assimilation of ice concentration and ice thickness





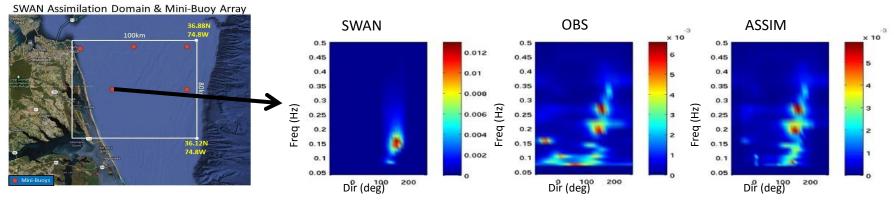




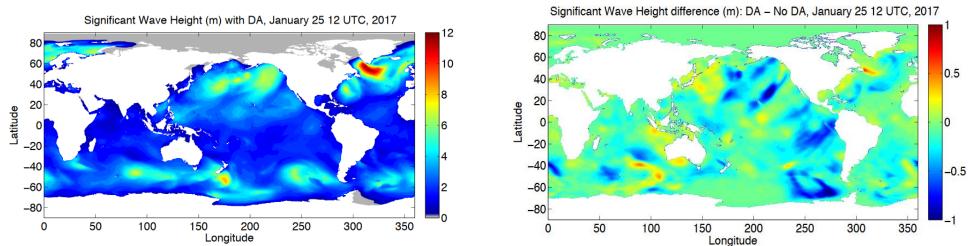


## **DA APPLICATIONS: WAVE**

SWAN 4DVAR (SWANFAR)



2DVAR HS WW3



4DVAR WW3: Developing tangent linear and adjoint models towards a WW3 4DVAR assimilation of wave spectra data



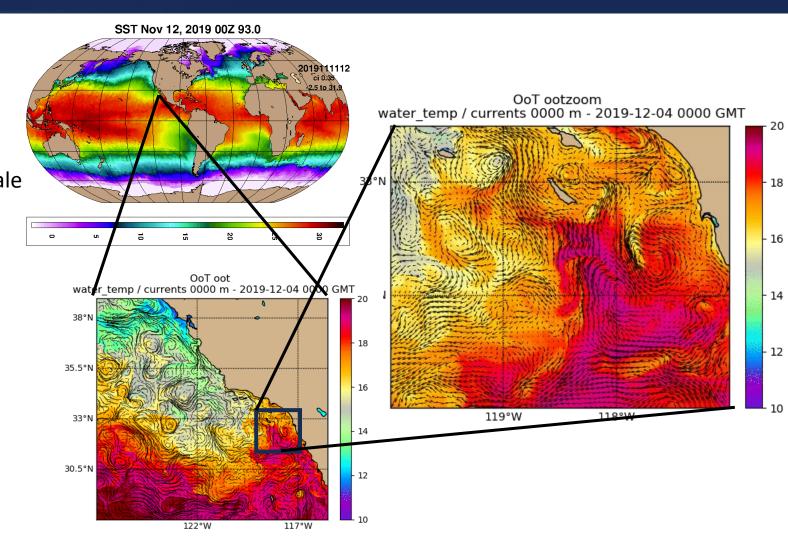








Global model: 3DVAR
SST, T/S profiles, SSH anomalies as synthetic T/S
profiles through ISOP
Large scale corrections (Rossby radius of
deformation as background error correlation scale



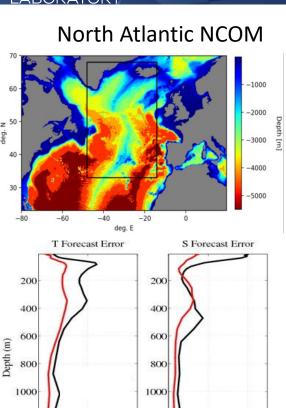












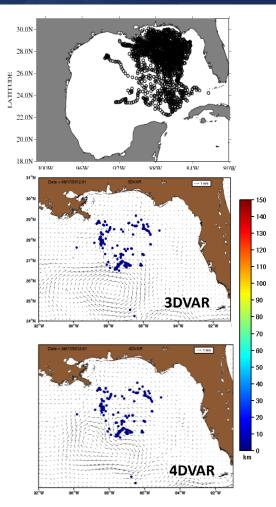
1200

1400

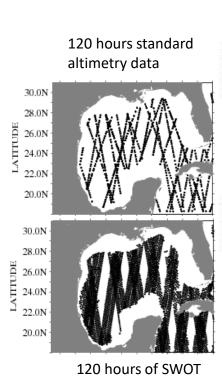
-3DV

-4DV

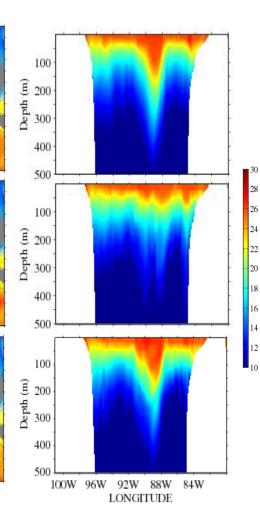
RMS Error (psu)



Color represents the distance between the model and real drifters over time



30.0N 28.0N 26.0N 24.0N 22.0N 20.0N 30.0N 28.0N 24.0N 20.0N 30.0N 28.0N 22.0N 20.0N 100W 96W 92W 88W 84W LONGITUDE





RMS Error (deg C)

1200

1400



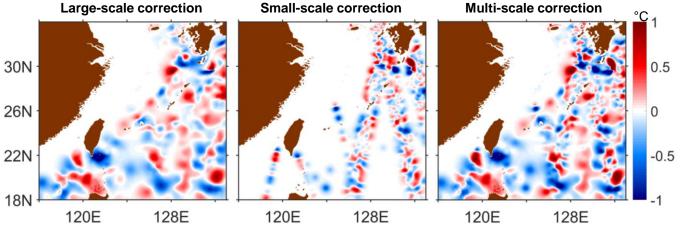






#### Multi-scale DA

$$\delta \mathbf{x} = \mathbf{B}_{L} \mathbf{H}_{L}^{\mathrm{T}} \left( \mathbf{H}_{L} \mathbf{B}_{L} \mathbf{H}_{L}^{\mathrm{T}} + \mathbf{R}_{L} \right)^{-1} \left( \mathbf{y}_{L} - \mathbf{H}_{L} \mathbf{x} \right)$$
$$+ \mathbf{B}_{S} \mathbf{H}_{S}^{\mathrm{T}} \left( \mathbf{H}_{S} \mathbf{B}_{S} \mathbf{H}_{S}^{\mathrm{T}} + \mathbf{R}_{S} \right)^{-1} \left( \mathbf{y}_{S} - \mathbf{H}_{S} \mathbf{x} \right)$$

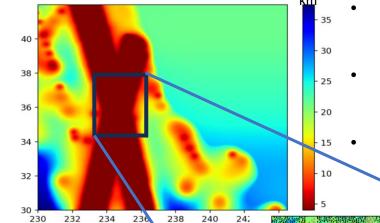


- Good step in the right direction
- Better solution than single-scale
- Scales are arbitrarily divided
- 2-step, but can we afford more?
- Does not account for all dense observations

#### Adaptive-scale DA

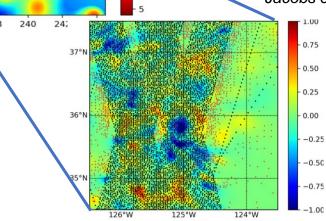
$$\delta \mathbf{x} = \mathbf{B}\mathbf{H}^{\mathrm{T}} \left( \mathbf{H}\mathbf{B}\mathbf{H}^{\mathrm{T}} + \mathbf{R} \right)^{-1} \left( \mathbf{y} - \mathbf{H}\mathbf{x} \right)$$

$$\mathbf{B}(x, x') = V^{1/2}(x)C(x, x', l(x))V^{1/2}(x')$$



- Retain more observations for assimilation
- Provide corrections at smaller scales as observed
- Does not account for all dense observations

Jacobs et al. 2023





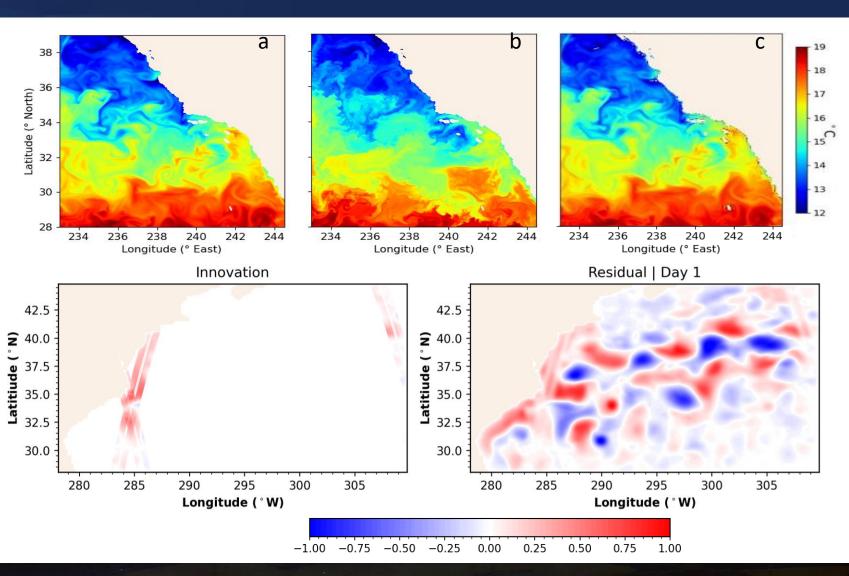






Dense observations: SST assimilation in NCOM Wavelets vs super-obs

Dense observations: SWOT assimilation in QG model









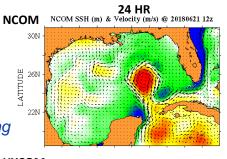


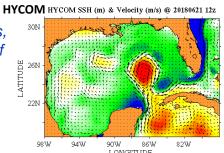


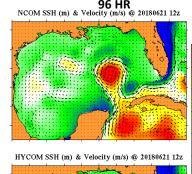
#### Hypothesis

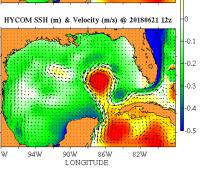
- NCOM and HYCOM are different numerical representations of the same equations
- 2. Given the same set of initial conditions (IC), boundary conditions (BC) and forcing (F) in the same domain with same horizontal resolution, both NCOM and HYCOM should produce similar solutions, over a typical assimilation time window of a few days.

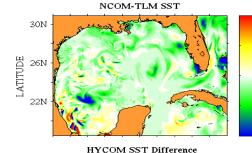
That is,  $N(I) \approx H(I)$ , where I=(IC, BC, F)  $N(I+\delta I) \approx H(I+\delta I)$ , and thus N'(I).  $\delta I \approx N(I+\delta I) - N(I) = H(I+\delta I) - H(I) \approx H'(I)$ .  $\delta I$ , hence  $(N')^T \approx (H')^T$ 







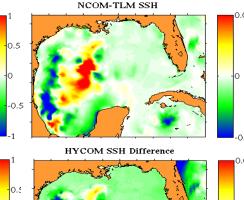


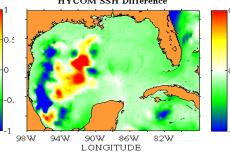


90W

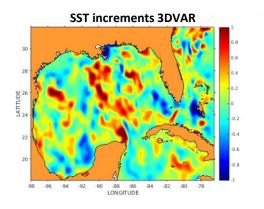
LONGITUDE

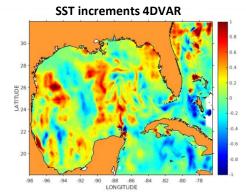
86W





- Interpolate z-level output to sigma-Z levels for NCOM and 4DVAR (IC).
- 2. Run NCOM forecast (to be used as background state for TLM-adjoint)
- 3. Run NCODA prep (to gather observations and calculate Obs-HYCOM innovations)
- 4. Run NCOM-based 4DVAR
- 5. Interpolate 4DVAR increments from sigma-Z to z-levels
- 6. Convert outputs into file format expected by HYCOM for model updating
- Run HYCOM forecast















Configure the existing 4DVAR system for the Navy Coastal Ocean Model (NCOM) to run in single precision instead of double precision, following the work Hatfield et al (2000).

Compared to the double precision, the single precision provides same accuracy and number of iterations, but much lower computational cost (wall clock time).

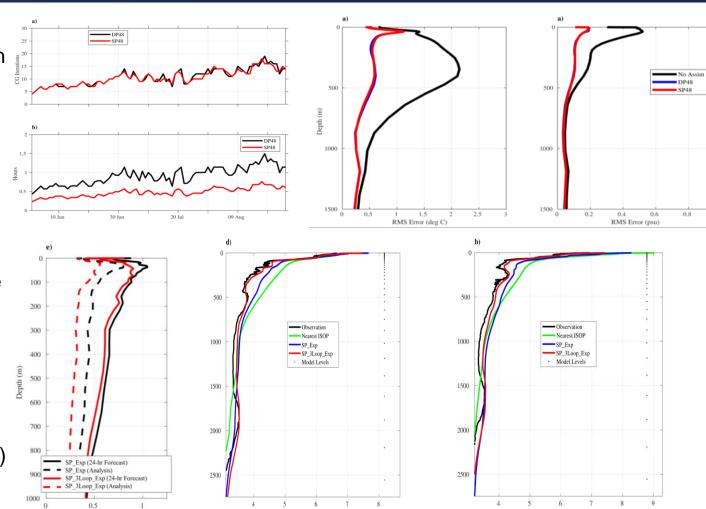
The computational savings with the single precision are invested in outer loops of the 4DVAR system.

Instead of assimilating all observations at once in one loop, 3 outer loops as follows:

Loop 1: SST assimilation

Loop 2: SSHA assimilation via synthetics (needs loop 1)

Loop 3: in-situ profiles









Temperature (deg C)

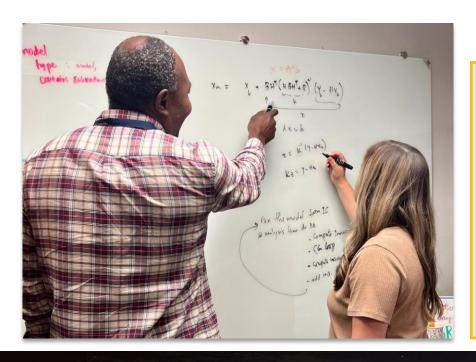


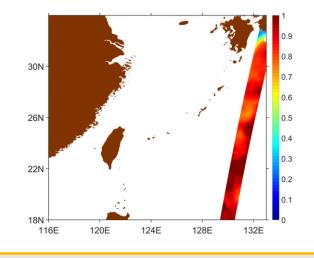


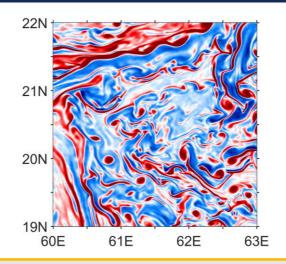
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## Ocean Dynamics and Prediction Branch

U.S. Naval Research Laboratory Stennis Space Center, MS







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