



In partnership with



Learning from (sparse) observations through the lens of models

*Patrick Heimbach &
The DJ4Earth & ECCO groups*

The University of Texas at Austin



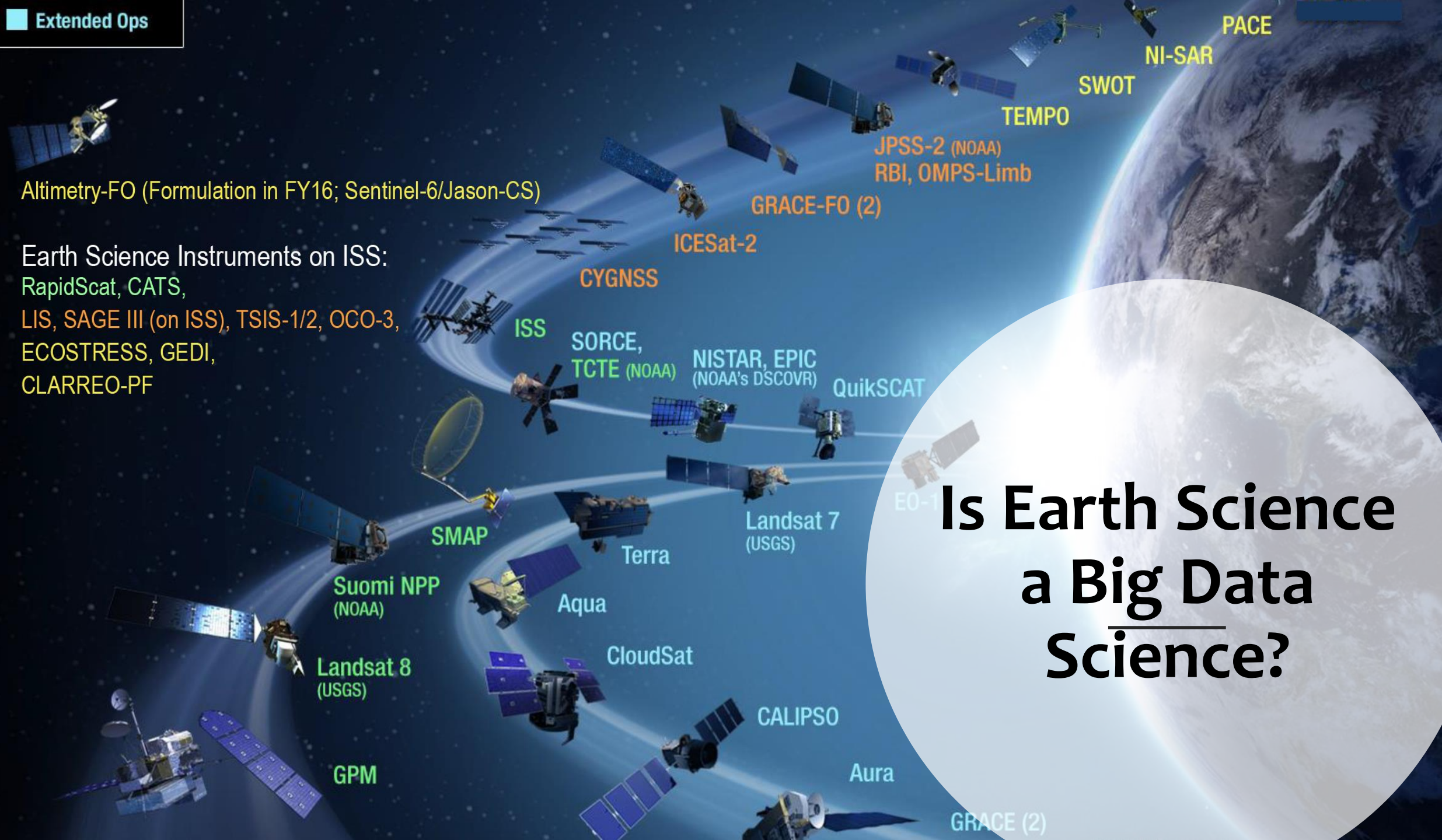
ODEN INSTITUTE

FOR COMPUTATIONAL ENGINEERING & SCIENCES



Altimetry-FO (Formulation in FY16; Sentinel-6/Jason-CS)

Earth Science Instruments on ISS:
RapidScat, CATS,
LIS, SAGE III (on ISS), TSIS-1/2, OCO-3,
ECOSTRESS, GEDI,
CLARREO-PF



Is Earth Science
a Big Data
Science?



PACE

NI-SAR

SWOT

TEMPO

JPSS-2 (NOAA)
RBI, OMPS-Limb

GRACE-FO (2)

ICESat-2

CYGNSS

ISS

SORCE,
TCTE (NOAA)

NISTAR, EPIC
(NOAA's DSCOVR)

QuikSCAT

EO-1

Landsat 7
(USGS)

SMAP

Terra

Suomi NPP
(NOAA)

Aqua

Landsat 8
(USGS)

CloudSat

CALIPSO

GPM

Aura

GRACE (2)

**Is Oceanography
a “big data”
science?**

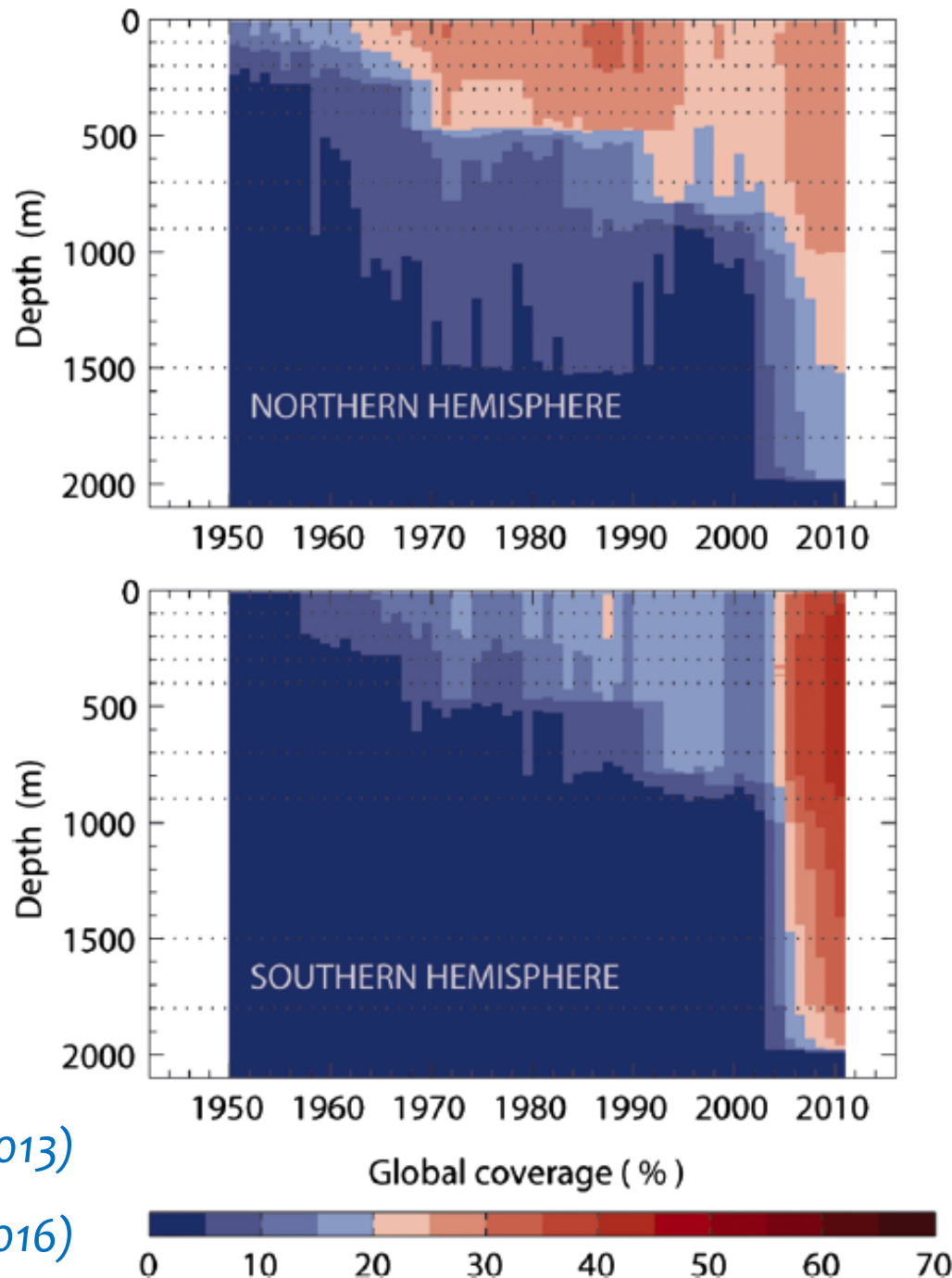
Yes & No ...

Oceanography: A sparse data problem ...

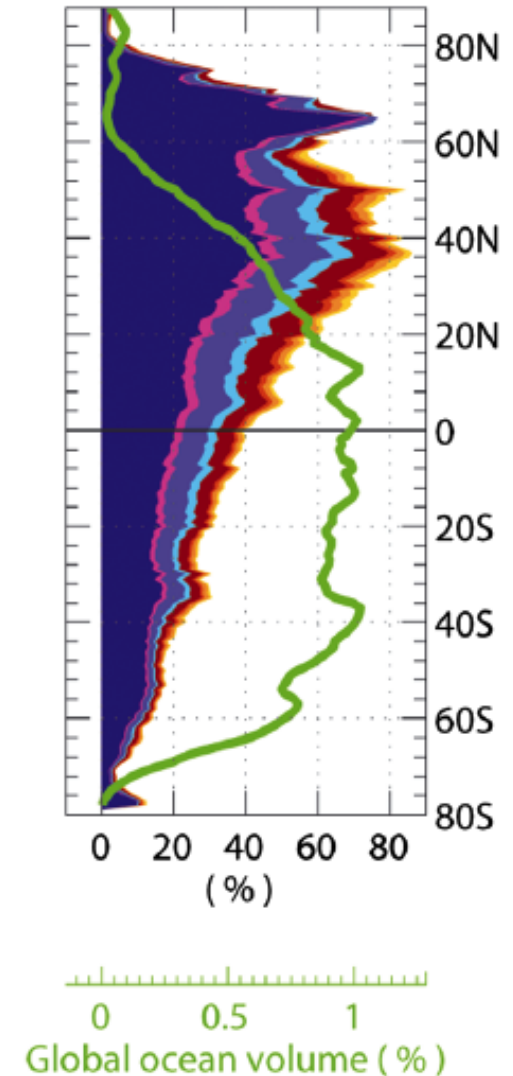
Observational sampling
coverage for ocean
temperature in the
upper 2000 m
1950 – 2010
(mean ocean depth:
~ 3900 m)

Abraham et al., Rev. Geophys. (2013)

Wunsch, Annual Reviews (2016)

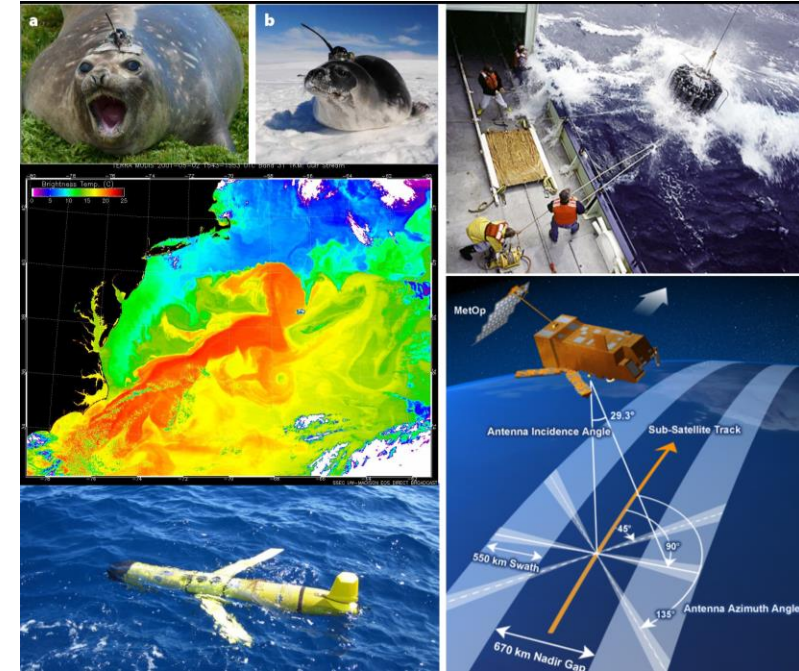


Mean zonal coverage
(1950–2011)



Two incomplete
knowledge
reservoirs

an eclectic, patchy, heterogeneous
observing system



numerical models

that require
uncertain
inputs



Parameter & state estimation

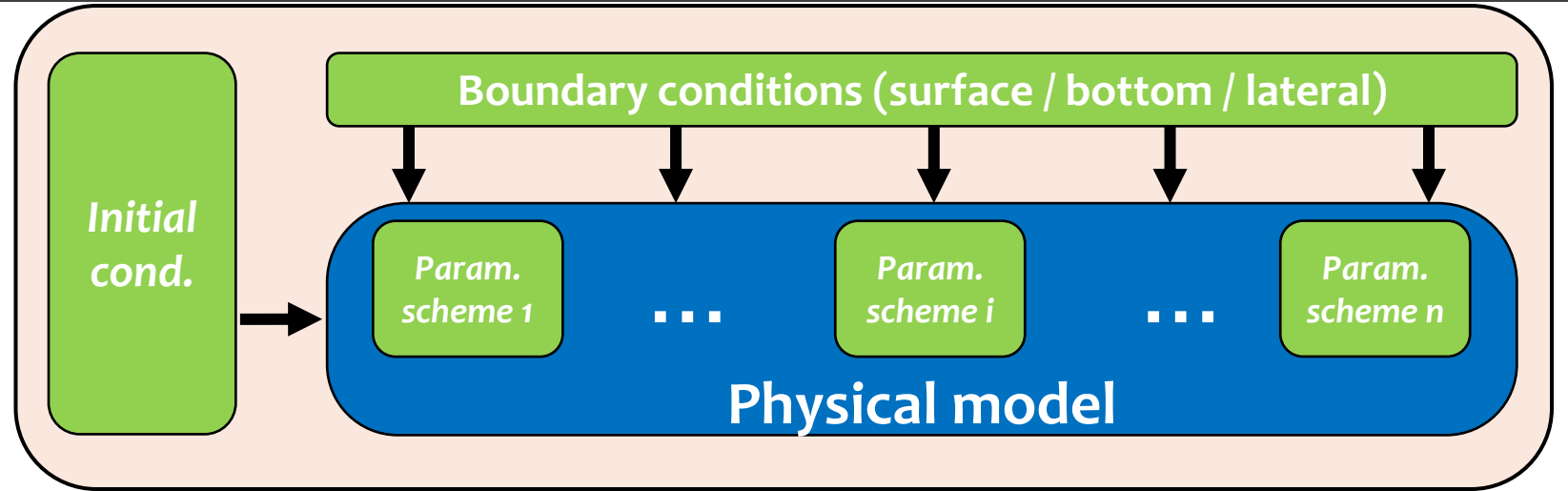
The data assimilation / inverse method is learning from ...

- a set of **usually sparse, heterogeneous** observations
- ... AND known (albeit uncertain) physics/dynamics,
- ... by solving a gigantic least-squares model-data misfit minimization

The background features a dark grey color with several concentric, overlapping circles in a lighter grey shade. A single dashed white line also follows a similar circular path, slightly offset from the solid lines.

What do we mean by
“Learning”?

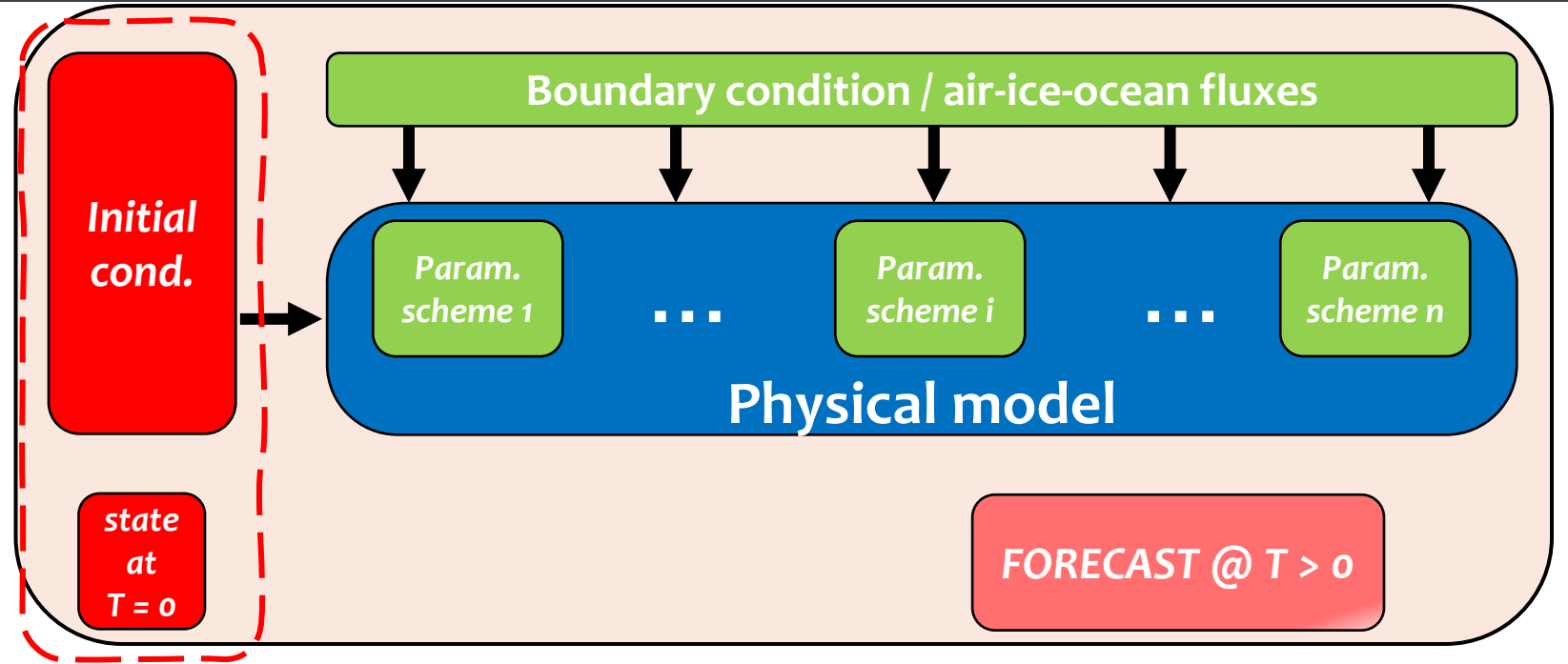
Learn ...



Learn model initial conditions

Find best initial conditions that will produce optimal forecast ...

The **filtering** problem of optimal estimation & control

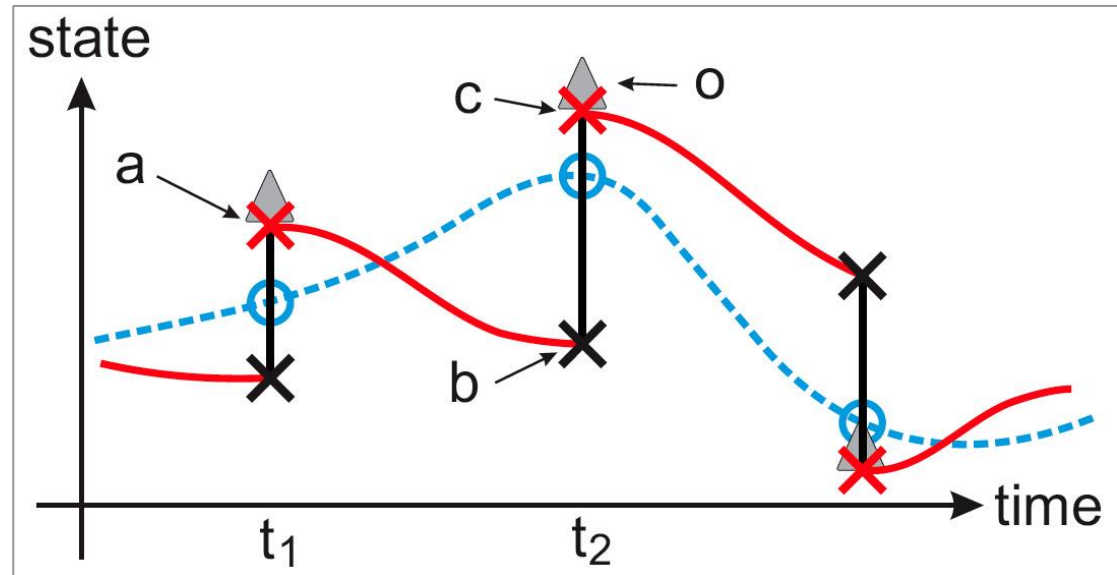
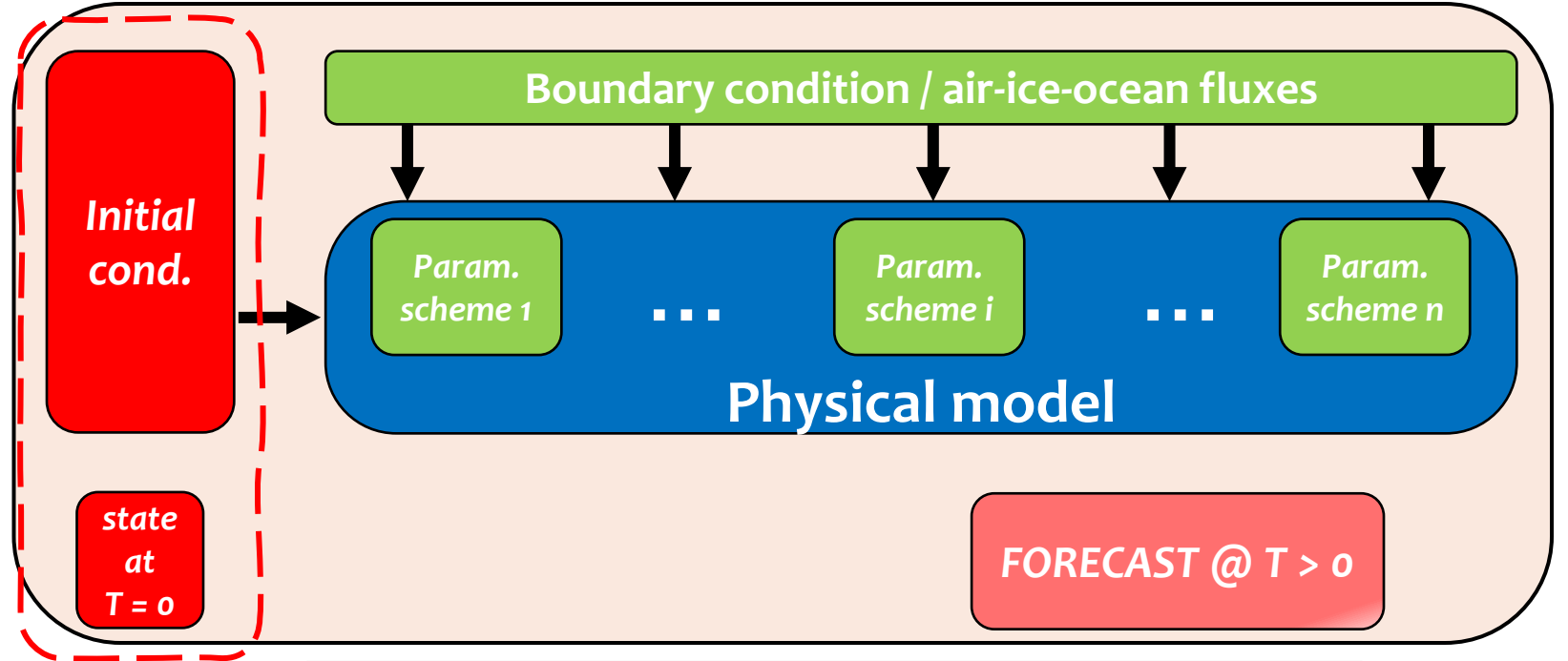


Learn model initial conditions

Find best initial conditions that will produce optimal forecast ...

The **filtering** problem of optimal estimation & control

Initialization for prediction/extrapolation as practiced in short-term **weather & ocean prediction**

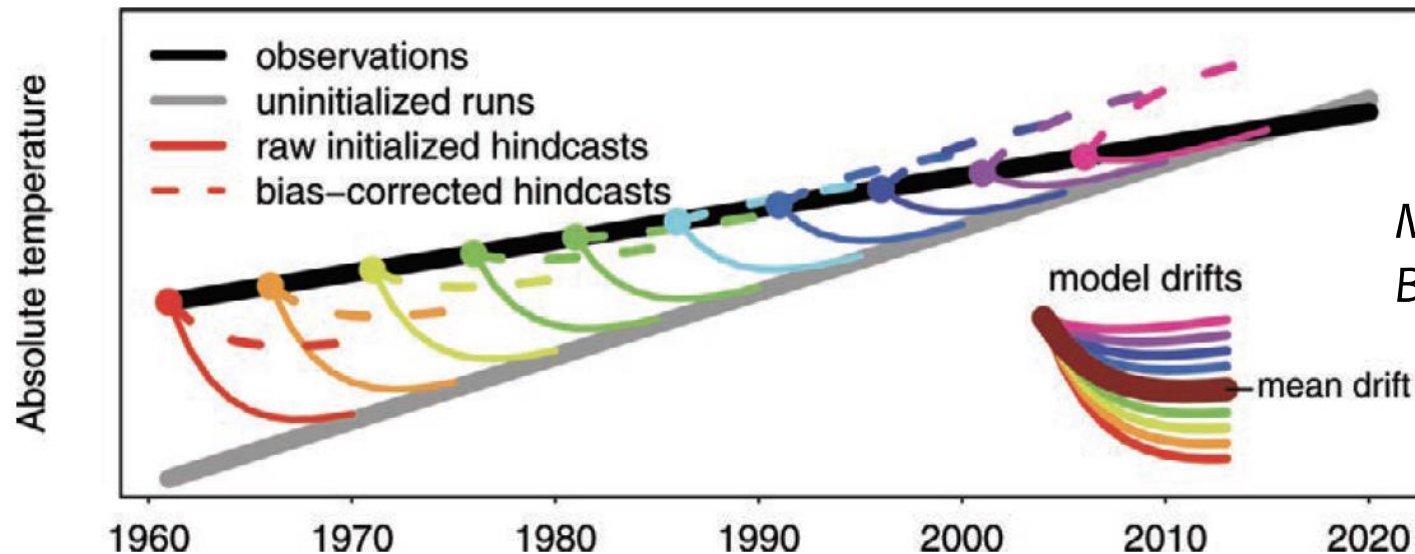
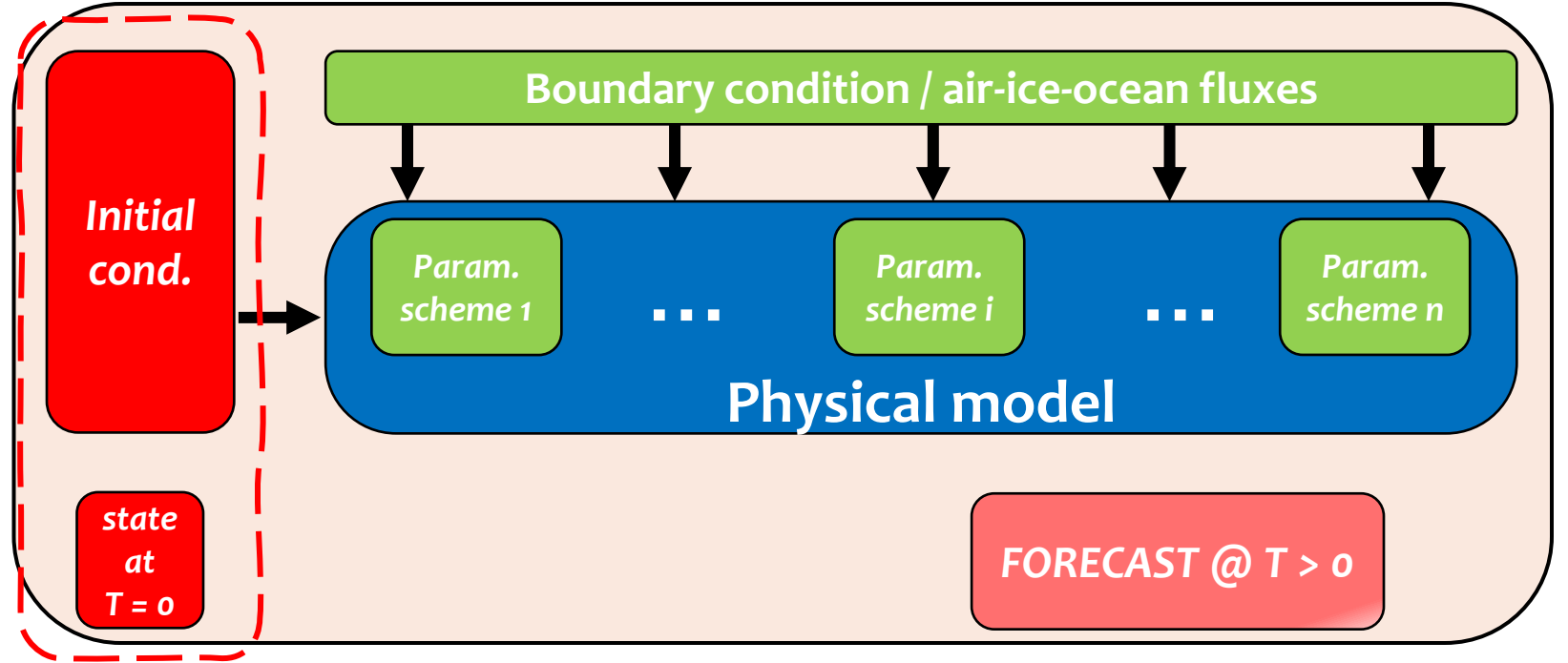


Learn model initial conditions

Find best initial conditions that will produce optimal forecast ...

The **filtering** problem of optimal estimation & control

Initialization for prediction/extrapolation as practiced in **interannual to decadal prediction**

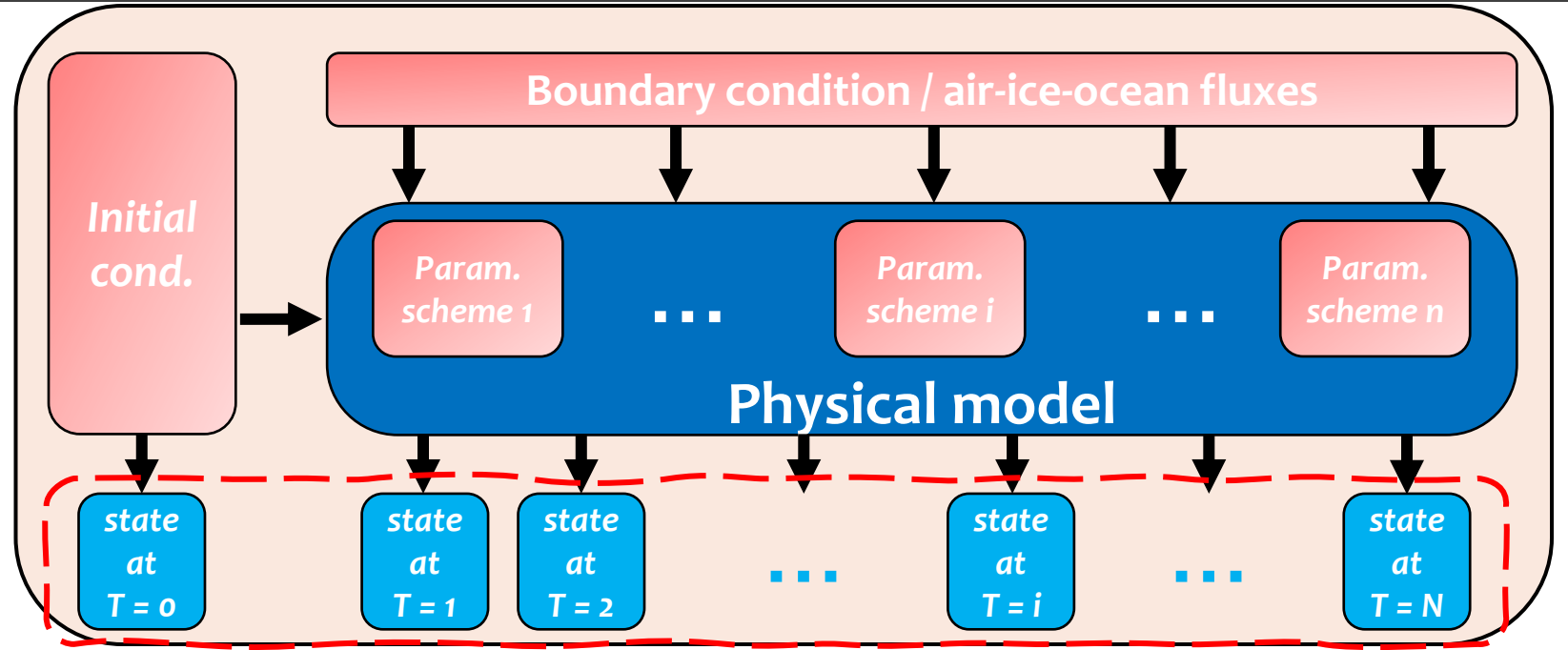


Meehl et al.
BAMS (2014)

Learn model time-evolving state

Find model inputs (in red) that produce the best dynamically consistent state

The smoothing problem of optimal estimation & control



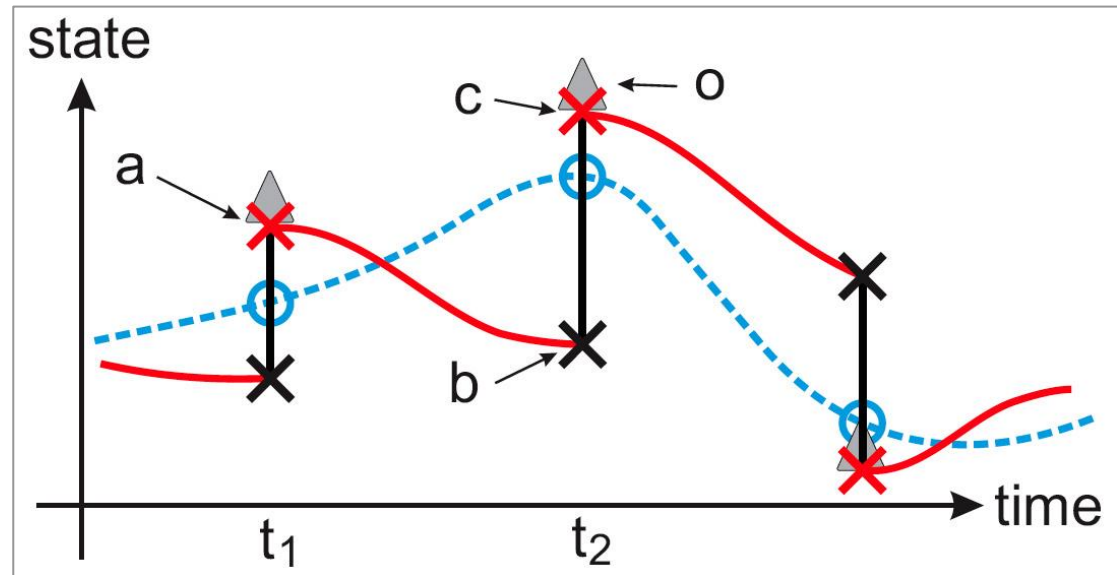
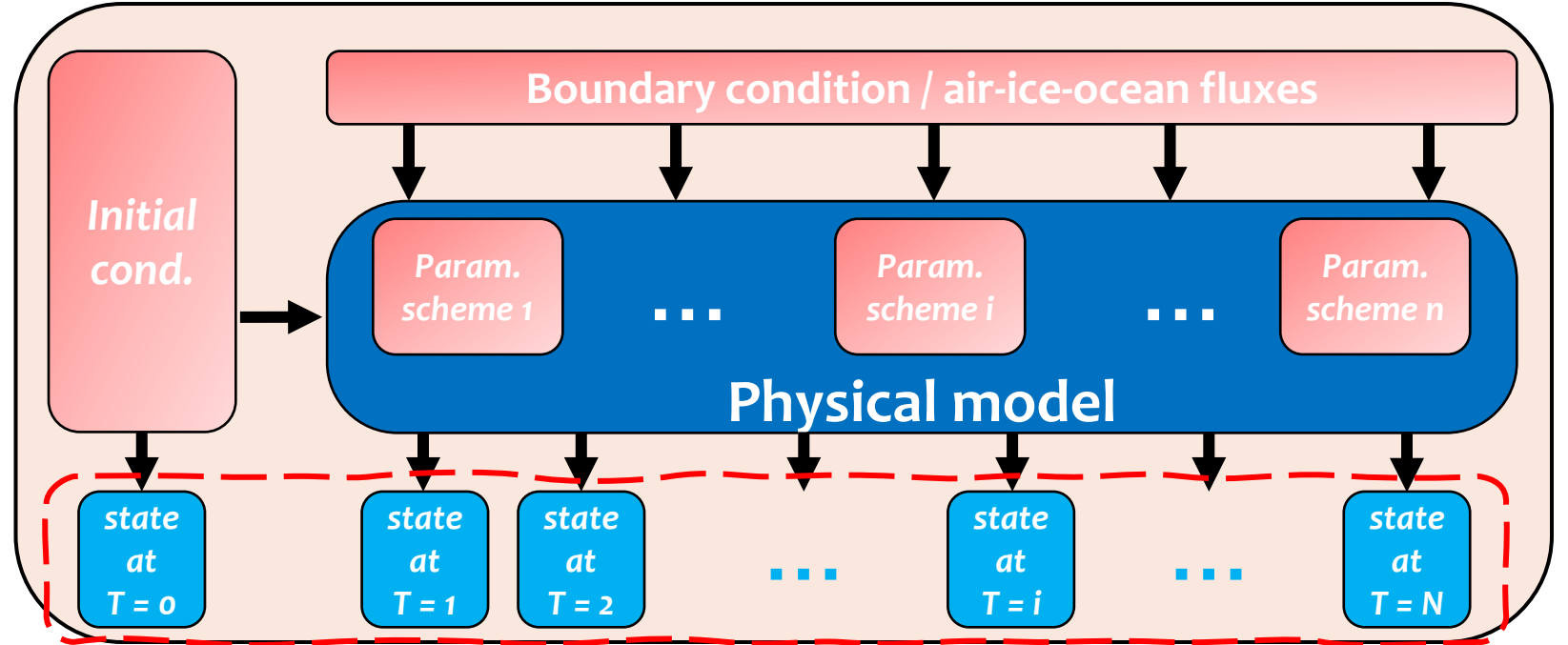
Learn model time-evolving state

Find model inputs (in red) that produce the best dynamically consistent state

The smoothing problem of optimal estimation & control

State & parameter estimation for:

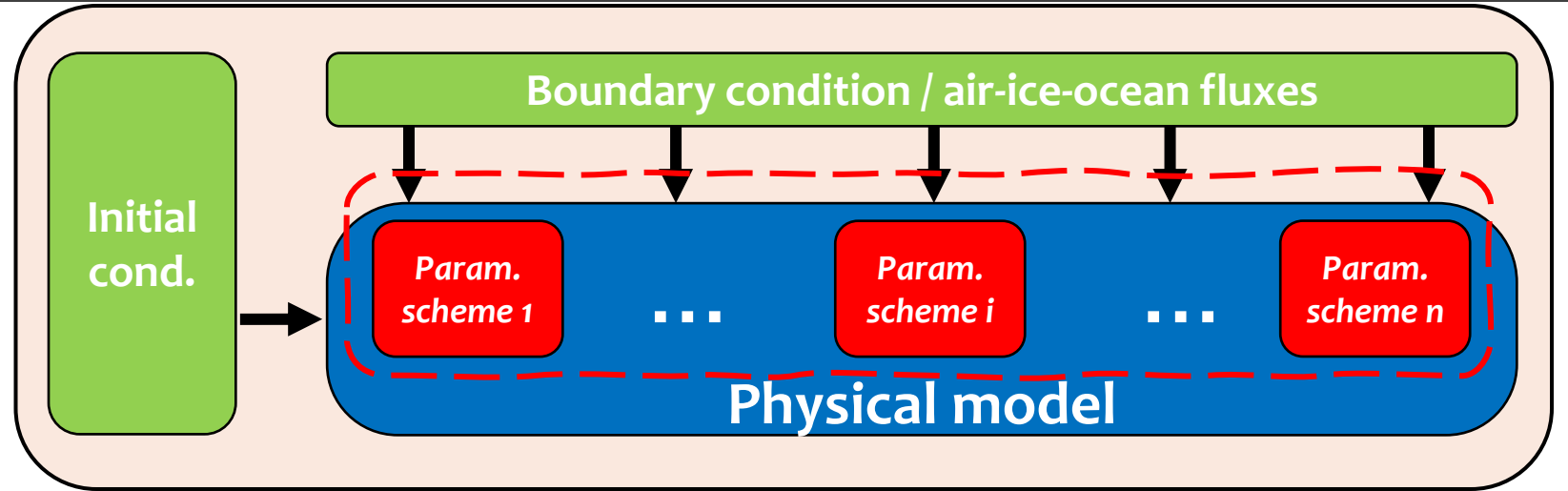
- Interpolation/reconstruction
- (transient calibration)



Learn model parameters

Physical model has many empirical parameters:

- constitutive laws
- subgrid-scale parameterization schemes

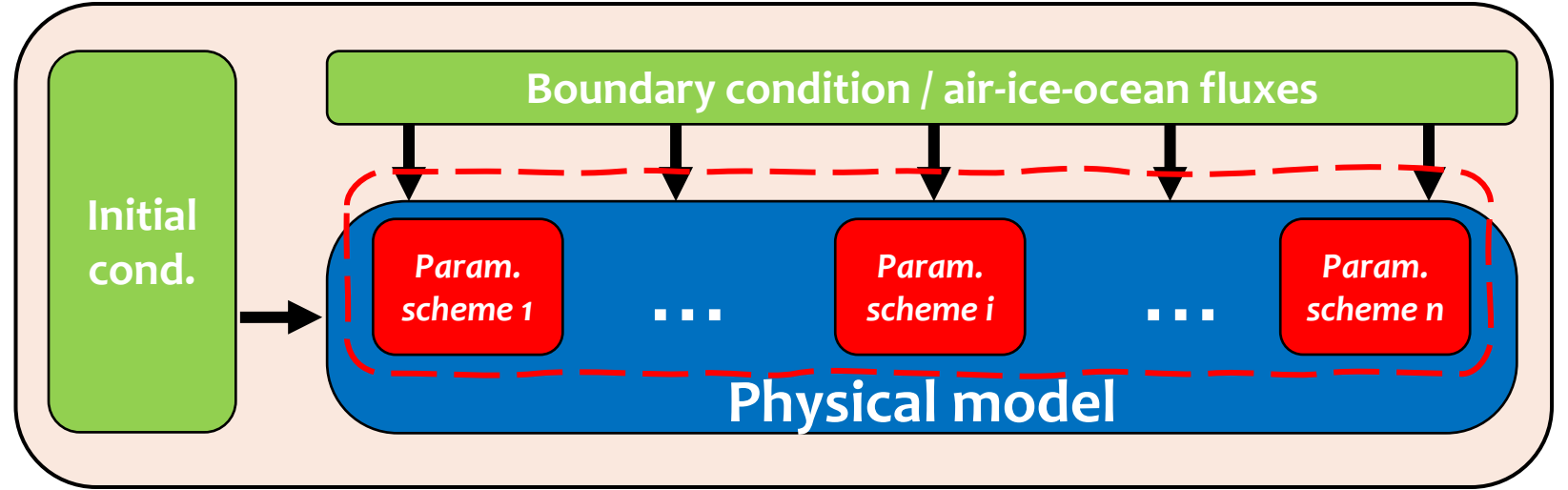


Learn model parameters

Physical model has many empirical parameters:

- constitutive laws
- subgrid-scale parameterization schemes

parameter estimation using observations is essential



THE ART AND SCIENCE OF CLIMATE MODEL TUNING

BAMS

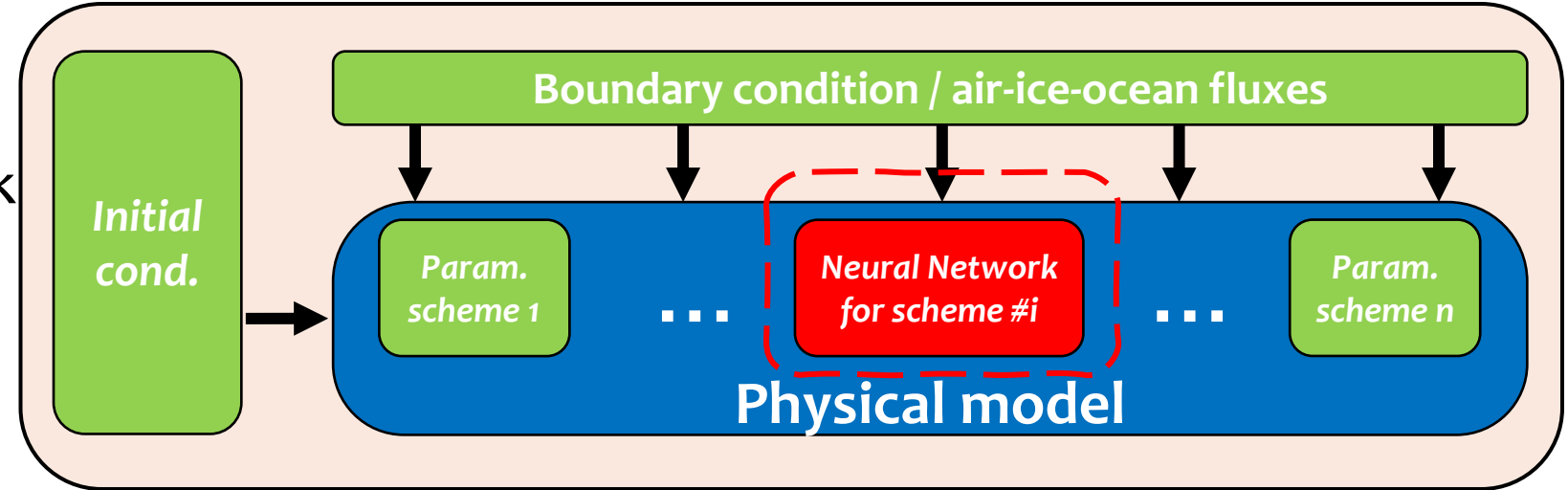
FRÉDÉRIC HOURDIN, THORSTEN MAURITSEN, ANDREW GETTELMAN, JEAN-CHRISTOPHE GOLAZ, VENKATRAMANI BALAJI, QINGYUN DUAN, DORIS FOLINI, DUOYING JI, DANIEL KLOCKE, YUN QIAN, FLORIAN RAUSER, CATHERINE RIO, LORENZO TOMASSINI, MASAHIRO WATANABE, AND DANIEL WILLIAMSON

We survey the rationale and diversity of approaches for tuning, a fundamental aspect of climate modeling, which should be more systematically documented and taken into account in multimodel analysis.

Learn surrogate (e.g., NN) of model's parameterization scheme

Parameterization scheme(s)
is replaced by neural network

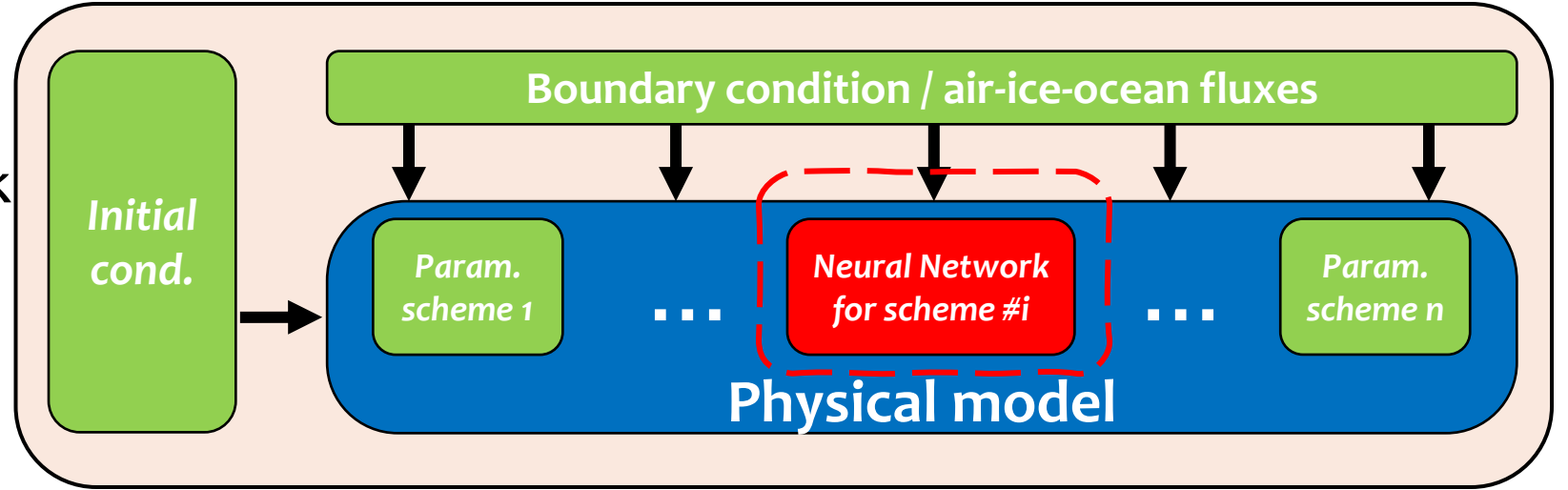
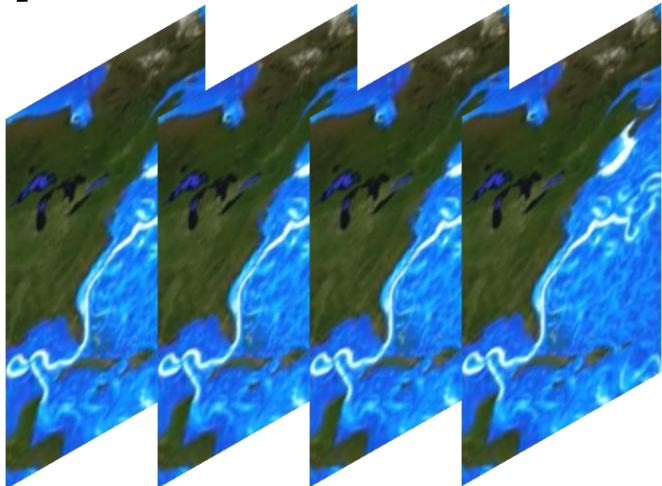
NN is trained on high-fidelity simulation data which resolve scales to be parameterized



Learn surrogate (e.g., NN) of model's parameterization scheme

Parameterization scheme(s) is replaced by neural network

NN is trained on high-fidelity simulation data which resolve scales to be parameterized

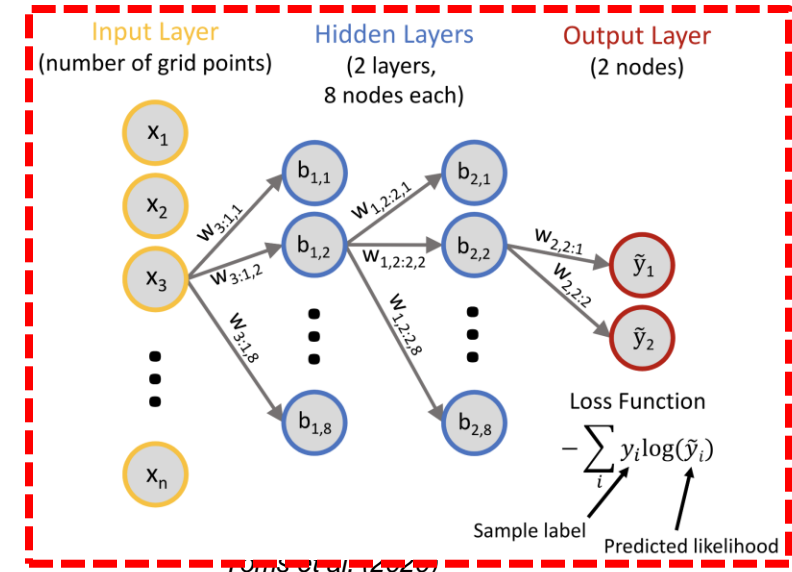


$$\frac{\partial \bar{\Phi}}{\partial t} + (\bar{\mathbf{u}} \cdot \nabla) \bar{\Phi} = \nabla \cdot (\kappa \nabla \bar{\Phi}) + \bar{F}_\Phi + \boxed{\nabla \cdot \mathbf{S}}$$

$$\boxed{\nabla \cdot \mathbf{S}} = \nabla \cdot (\bar{\mathbf{u}} \bar{\Phi} - \bar{\mathbf{u}} \bar{\Phi}) =$$

a priori / offline learning

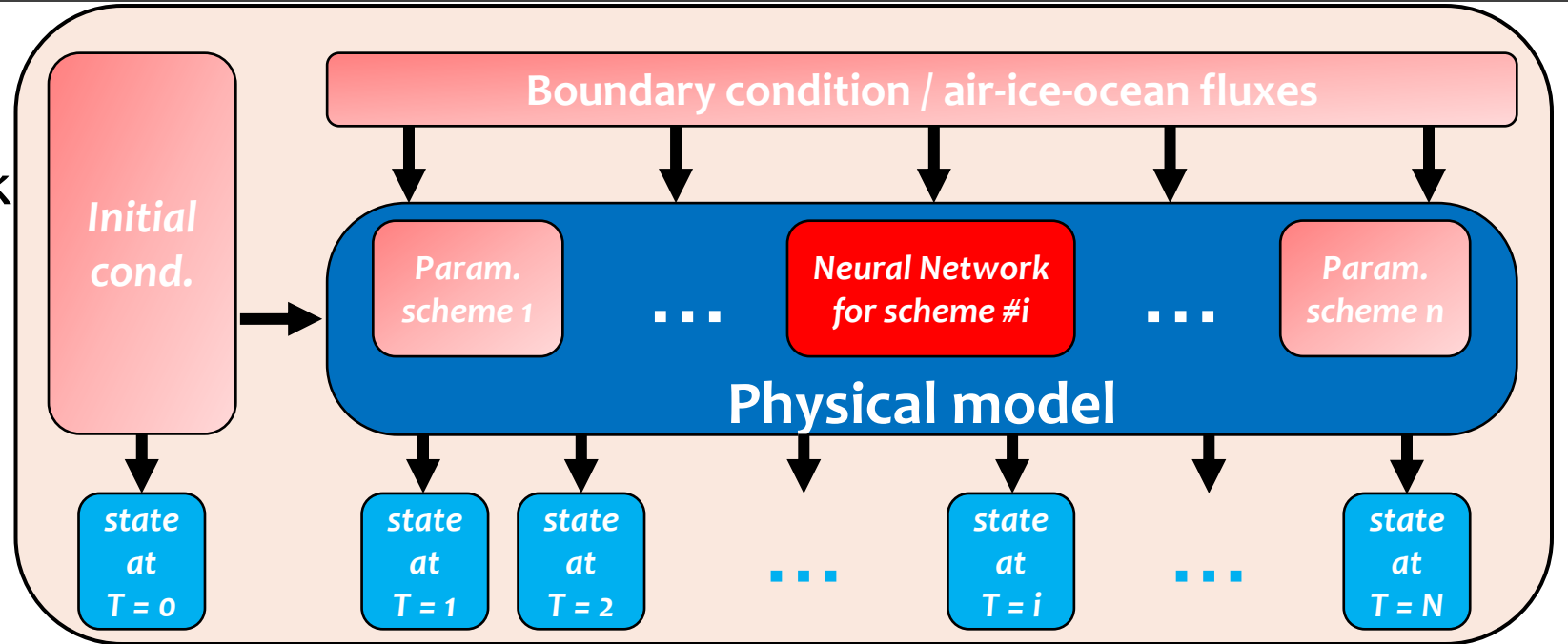
Frezat et al. (2019), Zanna & Bolton (2021)



Learn hybrid physical/surrogate (NN) model

Parameterization scheme(s)
is replaced by neural network

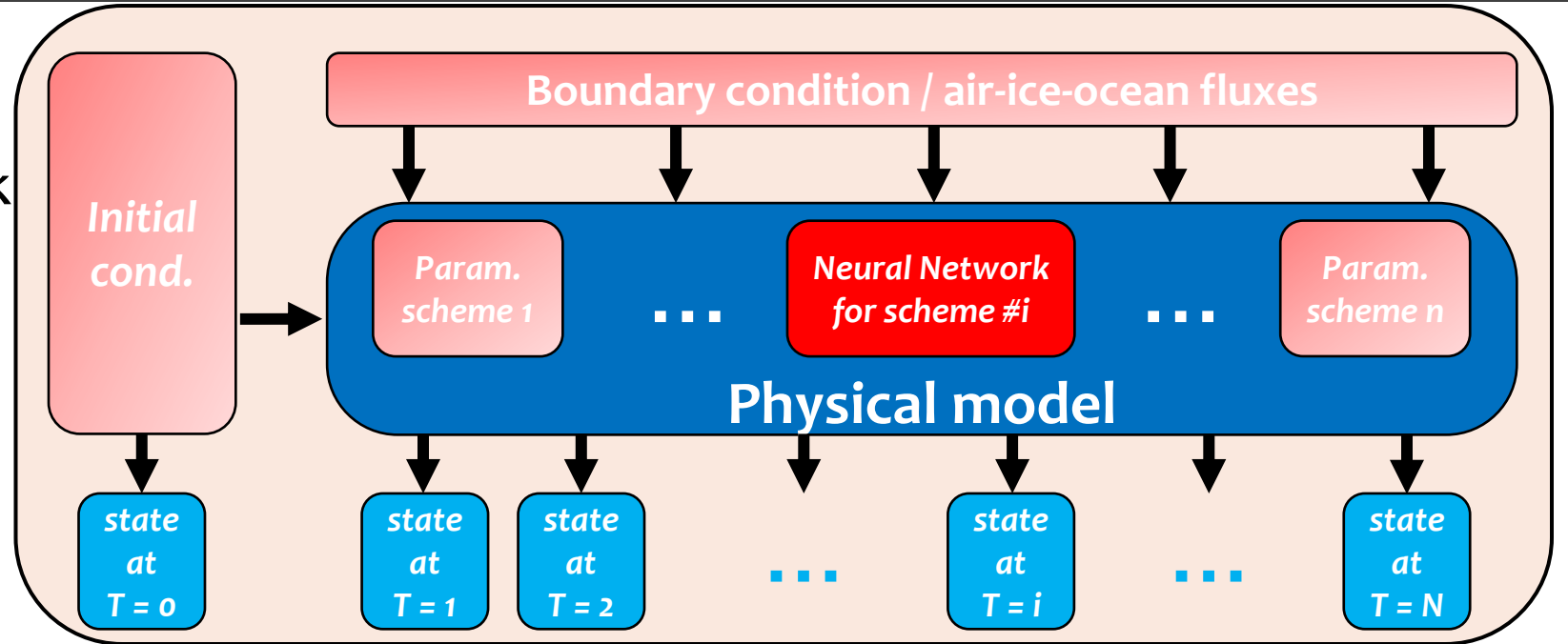
**Training of the NN is
part of “training” of
the physical model
on state variables**



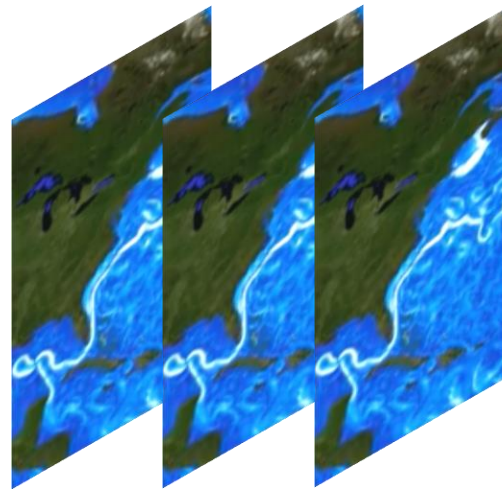
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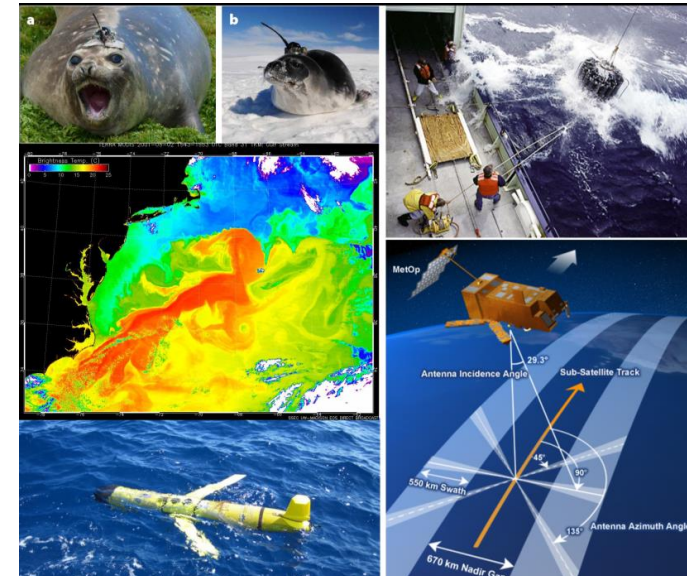
**Training of the NN is
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the physical model
on state variables**



**a posteriori / full-model
/ online / end-to-end
learning**



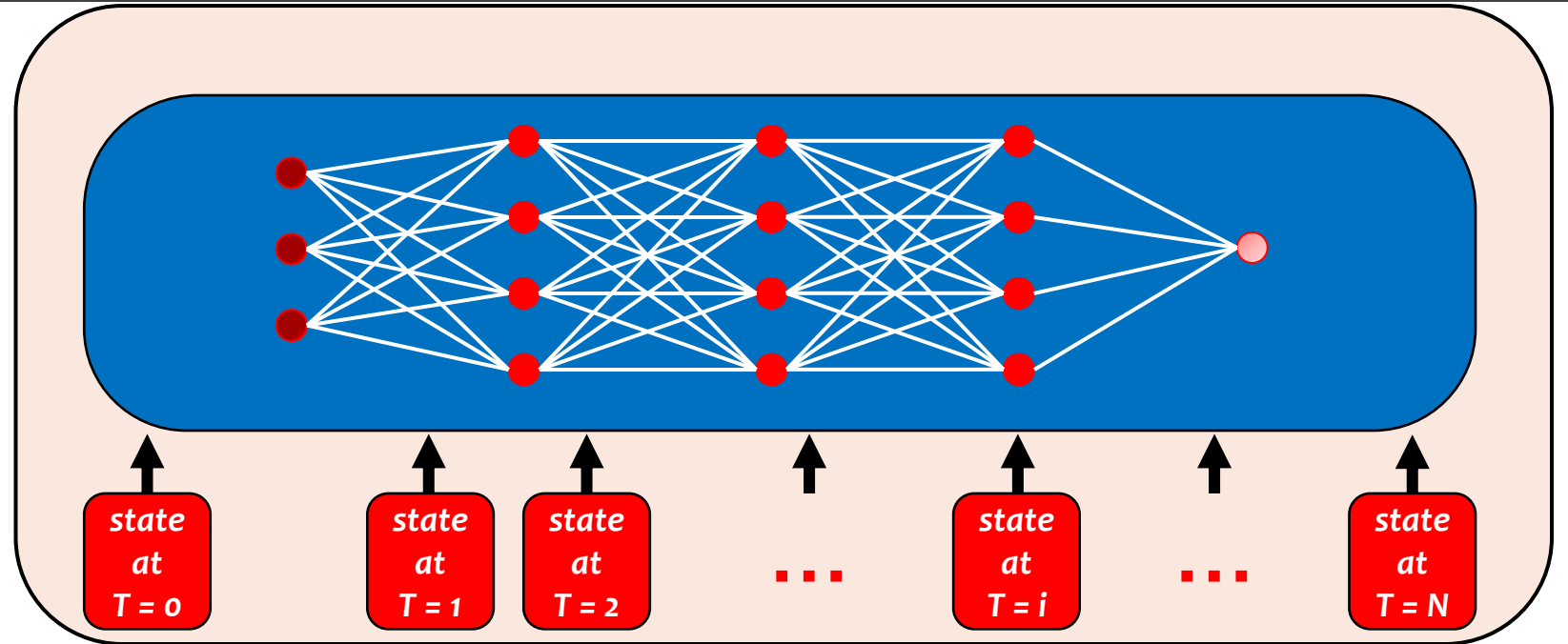
+



Learn surrogate (e.g., NN) of the entire physical model

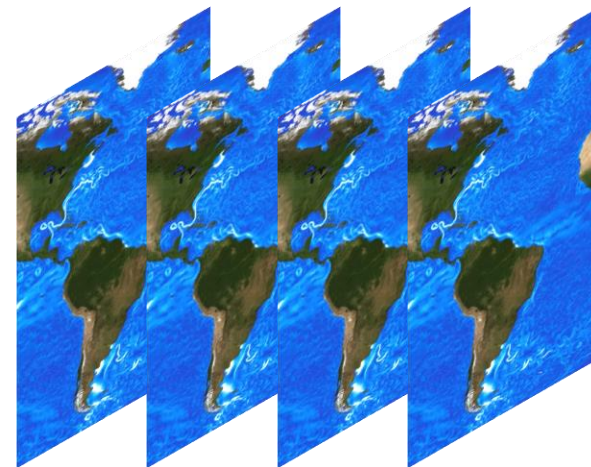
Physical model is replaced entirely by surrogate model, e.g., neural network (NN):

purely data-driven learning



Weights of neural network trained on simulated model states, either

- **high-fidelity models**
- or
- **reanalyses**



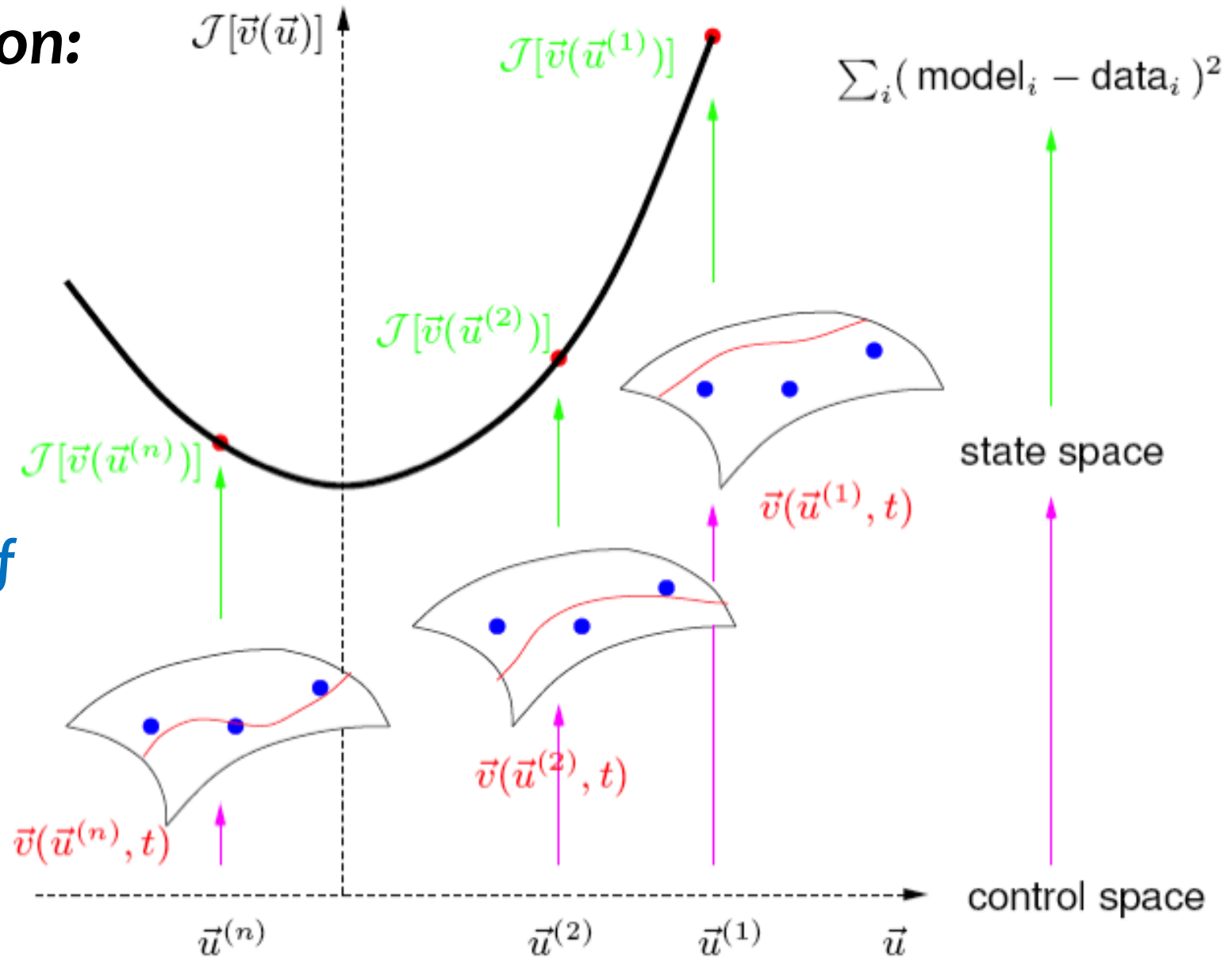
A key unifying computational framework of “learning from data”

Gradient-based optimization:

- inversion (physical models)
 - seek uncertain input / control variables / parameters
- training (neural networks)
 - seek uncertain weights of NN representation

Adjoint / backpropagation

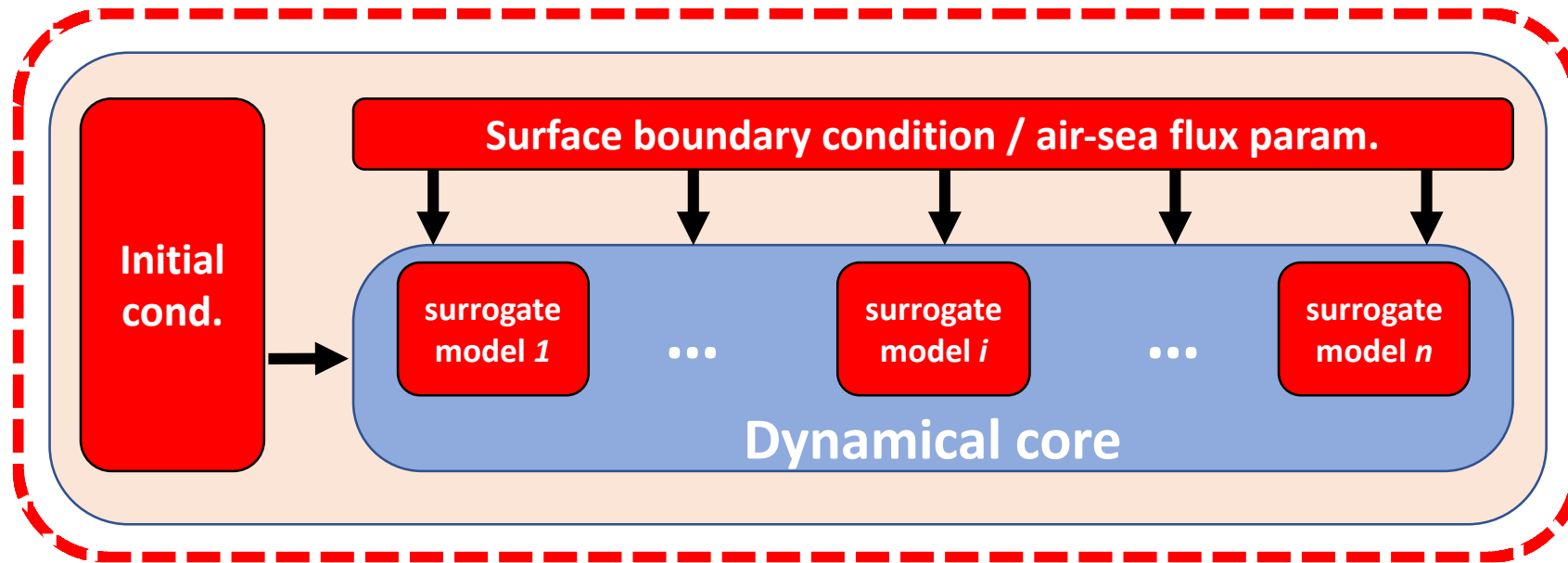
essential tool for computing high-dimensional gradients!



Full-model learning

Can we integrate the
surrogate model training
within full-model calibration

An end-to-end adjoint enables full-model calibration & initialization



Here: use of full-model [differentiable programming](#) to

- replace parts of model by appropriate surrogates
- use all available observations to train/calibrate all uncertain variables
- combines inverse modeling and ML in [end-to-end learning](#)

relies on general-purpose automatic differentiation (AD)

Home

Welcome to Differentiable programming in Julia for Earth system modeling (DJ4Earth)

Cyberinfrastructure for Sustained Scientific Innovation (CSSI)



<https://DJ4Earth.github.io>

NSF CSSI: **DJ4Earth**

Convergence of Bayesian inverse methods and scientific machine learning through universal differentiable programming

Since 2023 the idea of differentiable programming has taken off ...

Geosci. Model Dev., 16, 3123–3135, 2023

<https://doi.org/10.5194/gmd-16-3123-2023>

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Geoscientific
Model Development



Differentiable programming for Earth system modeling

Maximilian Gelbrecht^{1,2}, Alistair White^{1,2}, Sebastian Bathiany^{1,2}, and Niklas Boers^{1,2,3}

¹Earth System Modelling, School of Engineering and Design, Technical University of Munich, Munich, Germany

²Potsdam Institute for Climate Impact Research, Potsdam, Germany

³Department of Mathematics and Global Systems Institute, University of Exeter, Exeter, UK

Since 2023 the idea of differentiable programming has taken off ...

Geosci. Model Dev., 16, 3123–3135, 2023

<https://doi.org/10.5194/gmd-16-3123-2023>

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Geoscientific
Model Development

Open Access



<https://doi.org/10.1038/s43017-023-00450-9>



Differentiable programming

Maximilian Gelbrecht^{1,2}, Alistair White^{1,2}, Sebastian

¹Earth System Modelling, School of Engineering and De

²Potsdam Institute for Climate Impact Research, Potsdam,

³Department of Mathematics and Global Systems Institute,

nature reviews earth & environment

Perspective

Differentiable modelling to unify machine learning and physical models for geosciences

A list of authors and their affiliations appears at the end of the paper

Since 2023 the idea of differentiable programming has taken off ...

Geosci
https://
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the
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135, 2023

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Model Development

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<https://doi.org/10.1038/s43017-023-00450-9>

Check for updates

arXiv > math > arXiv:2406.09699

Mathematics > Numerical Analysis

[Submitted on 14 Jun 2024]

Differentiable Programming for Differential Equations: A Review

Facundo Sapienza, Jordi Bolibar, Frank Schäfer, Brian Groenke, Avik Pal, Victor Boussange, Patrick Heimbach, Giles Hooker, Fernando Pérez, Per-Olof Persson, Christopher Rackauckas

Maximilian ...

¹Earth System Modelling
²Potsdam Institute for Climate
³Department of Mathematics and Global

mode

A list of authors and their affiliations

...lling to unify
physical

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arXiv > math > 2311.125, 2023

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<https://doi.org/10.1038/s43017-023-00450-9>

Check for updates

Article

Neural general circulation models for weather and climate

<https://doi.org/10.1038/s41586-024-07744-y>

Received: 13 November 2023

Accepted: 15 June 2024

Published online: 22 July 2024

Dmitrii Kochkov^{1,6}✉, Janni Yuval^{1,6}✉, Ian Langmore^{1,6}, Peter Norgaard^{1,6}, Jamie Smith^{1,6}, Griffin Mooers¹, Milan Klöwer², James Lottes¹, Stephan Rasp¹, Peter Düben³, Sam Hatfield³, Peter Battaglia⁴, Alvaro Sanchez-Gonzalez⁴, Matthew Willson⁴, Michael P. Brenner^{1,5} & Stephan Hoyer^{1,6}✉

A list of authors and their affiliations

...ge, Patrick Heimbach,

Differentiating a GPU-enabled climate model in Julia



Building on CiMA

CLIMATE MODELING ALLIANCE

A NEW APPROACH TO CLIMATE MODELING

CLIMATE MACHINE

SCALABLE PLATFORM

OPEN HUB

SCHMIDT FUTURES NSF DARPA HEISING-SIMONS FOUNDATION Audi Environmental Foundation

*Harness next-gen.
compute architecture*

TOOLBOX

JULIA: COME FOR THE SYNTAX, STAY FOR THE SPEED

Researchers often find themselves coding algorithms in one programming language, only to have to rewrite them in a faster one. An up-and-coming language could be the answer.

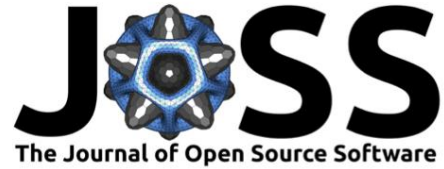
1 AUGUST 2019 | VOL 572 | NATURE

SIAM REVIEW
Vol. 59, No. 1, pp. 65–98

Julia: A Fresh Approach to Numerical Computing*

ClimaOcean.jl:

Ocean model component of the *Climate Model Alliance (CliMA)* model

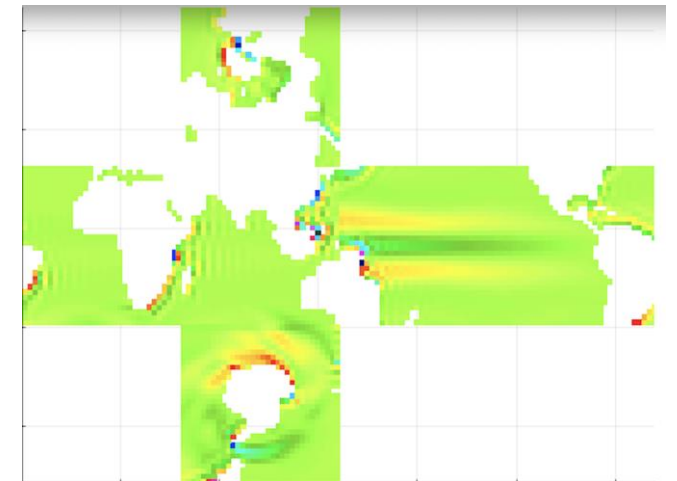
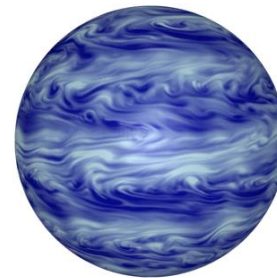
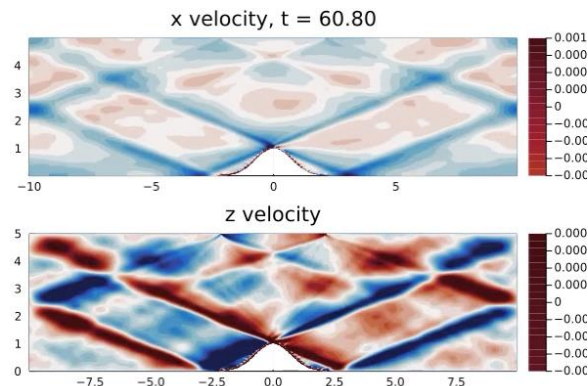
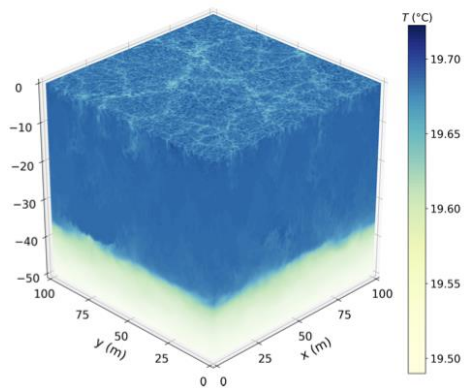


Oceananigans.jl: Fast and friendly geophysical fluid dynamics on GPUs

Ali Ramadhan¹, Gregory LeClaire Wagner¹, Chris Hill¹, Jean-Michel Campin¹, Valentin Churavy¹, Tim Besard², Andre Souza¹, Alan Edelman¹, Raffaele Ferrari¹, and John Marshall¹

¹ Massachusetts Institute of Technology ² Julia Computing, Inc.

- Finite volume, rotating, stratified fluids model for geophysical fluid dynamics (GFD).
- Written from scratch in Julia
- Multiple simulation options.
- GPU and CPU via kernel abstractions
- Parallelize using MPI.jl and multi-threading



<https://github.com/clima/Oceananigans.jl>

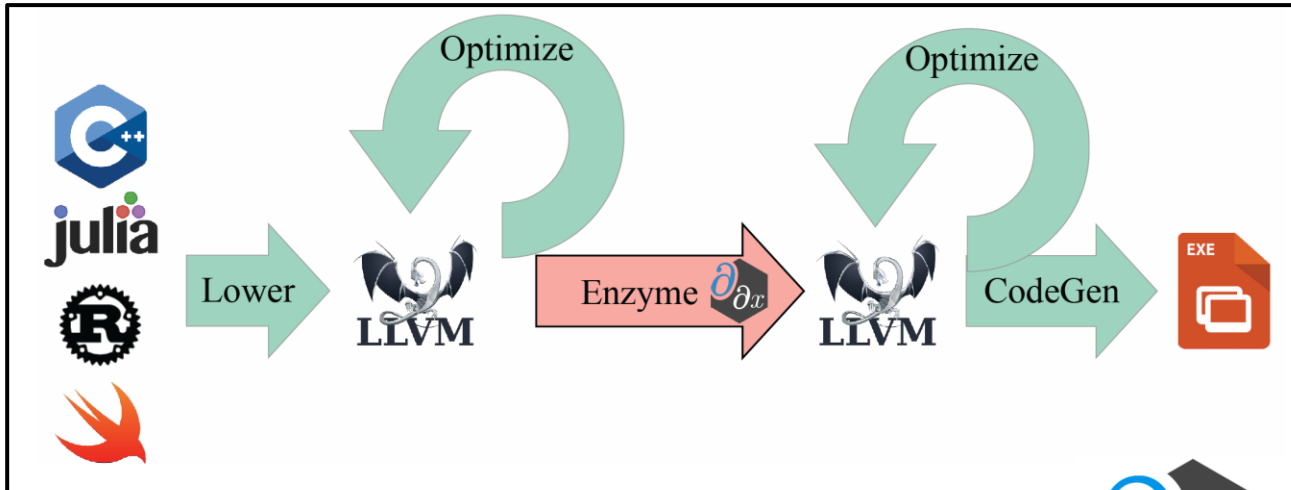
Differentiable programming for full-model / end-to-end learning

Differentiating GPU-enabled ocean model
in Julia via the AD tool *Enzyme.jl*

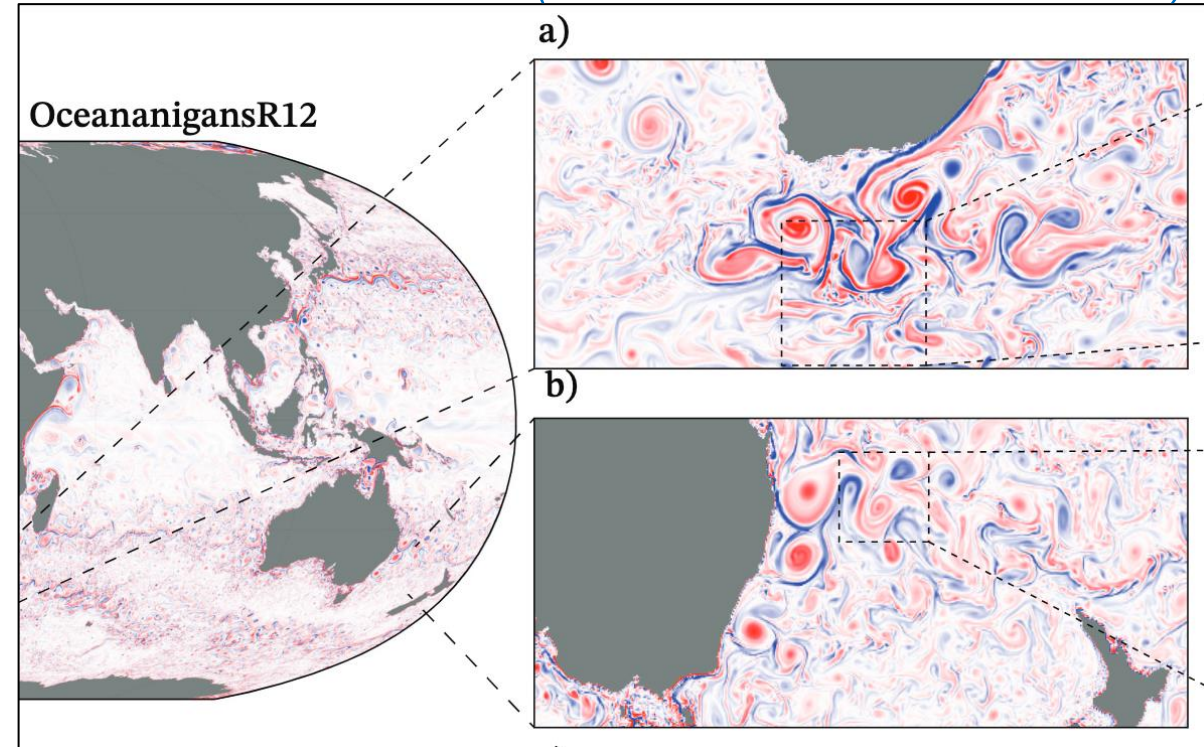
DJ4Earth



Oceananigans.jl
(Silvestri et al., arXiv, 2024)



Moses, Churavy, et al., SC'21



Three initial Earth system applications

Ocean

Sea ice

Ice sheets

S. Williamson

J. Kump

N. Loose

S. Silvestri

G. Wagner

C. Hill

M. Morlighem

C. Gong



- Bringing together concepts from ...
 - ... **big data science** & **sparse data science**
 - ... **computer science** & **computational science**
 - ... **scientific machine learning** & **simulation-based science**
- Sensitivity/gradient information is a powerful ingredient; obtained via
 - **differentiable programming**
 - **general-purpose automatic differentiation (AD)**

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24

ADVANCING OCEAN PREDICTION
SCIENCE FOR SOCIETAL BENEFITS

Thank you!